

Aim

To solve the algebraic explicit relations (or equations) used in chemical engineering problems using SCILAB

Problem statements

Exercise 1:

Use of `input` and `disp` commands in Dimensionless number calculations. Create a script file incorporating the above-mentioned commands to calculate the Reynolds, Prandtl, Nusselt, Grashof, Schmidt and Archimedes number in U.S. customary units as well as in SI units.

a) Calculation of Reynolds Number

$$N_{Re} = \frac{DV\rho}{\mu}$$

U.S. customary units

$$D = 3 \text{ in.} = \frac{3}{12} \text{ ft}$$

$$V = 6 \text{ ft/s}$$

$$\rho = 0.08 \text{ lbm/ft}^3$$

$$\mu = 0.015 \text{ cp} = (0.015)(0.000672) \text{ lbm/ft}\cdot\text{s}$$

$$N_{Re} = \frac{(3/12)(6)(0.08)}{(0.015)(0.000672)} = 11,904$$

SI units

$$D = (3)(0.0254) \text{ m}$$

$$V = (6)(0.3048) \text{ m/s}$$

$$\rho = (0.08)(16.018) \text{ kg/m}^3$$

$$\mu = (0.015)(0.001) \text{ kg/m}\cdot\text{s}$$

$$N_{Re} = \frac{(3 \times 0.0254) (6 \times 0.3048) (0.08 \times 16.018)}{(0.015) (0.001)} = 11,904$$

Similarly, try the following dimensionless numbers using the `input` and `disp` commands

Open SciNotes and type the following

```
D = input('Diameter, (ft) = ');
V = input('Velocity, (ft/s) = ');
Rho = input('Density, (lbm/cubic feet) = ');
Mu = input('Viscosity, (lbm/ft.s) = ');
disp(' ')
disp('Reynolds no. = ')
disp(D*V*Rho/Mu)
```

Press, Save and execute the function (Play button) in SCINOTES window and then goto console window. Provide the input values to execute the above function as given below:

```
-->exec('/Users/admin/Desktop/reynolds.sce', -1)
```

Diameter, (ft) = 3/12
 Velocity, (ft/s) = 6
 Density, (lbm/cubic feet) = 0.08
 Viscosity, (lbm/ft.s) = 0.015*0.000672

Reynolds no. =
 11904.762

Open SciNotes and type the following

```
D = input('Diameter, (m) = ');
V = input('Velocity, (m/s) = ');
Rho = input('Density, (kg/cubic meter) = ');
Mu = input('Viscosity, (kg/m.s) = ');
disp(' ')
disp('Reynolds no. = ')
disp(D*V*Rho/Mu)
```

Press, Save and execute the function (Play button) in SciNotes window and then goto console window. Provide the input values to execute the above function as given below:

```
-->exec('/Users/admin/Desktop/reynoldssi.sce', -1)
Diameter, (m) = 3*0.0254
Velocity, (m/s) = 6*0.3048
Density, (kg/cubic meter) = 0.08*16.018
Viscosity, (kg/m.s) = 0.015*0.001
```

Reynolds no. =
 11904.967

Exercise 2:

Calculation of a Prandtl Number

$$N_{Pr} = \frac{C_p \mu}{k}$$

U.S. customary units

$\gamma_p = 0.47$ Btu/lbm °F
 $\mu = 15$ centipoise = (15) (0.000672) (3600) lbm/ft-hr
 $k = 0.065$ Btu/hr-ft² (°F/ft)

$$N_{Pr} = \frac{(0.47) (15 \times 0.000672 \times 3600)}{0.065} = 262.4$$

SI units

$\gamma = (0.47)(4184)$ J/kg °C
 $\mu = (15)(0.001)$ kg/m-s
 $k = (0.065)(1.728)$ J/s-m² (°C/m)

$$N_{Pr} = \frac{(0.47) (4184) (15) (0.001)}{(0.065) (1.728)} = 262.6$$

Open SciNotes and type the following

```
Cp=input('Heat Capacity, (Btu/lbm deg. F) = ');
Mu=input('Viscosity, (lbm/ft h)=');
k=input('Thermal conductivity, (Btu/hr sq. ft)=');
disp(' ');
disp('Prandtl No. =');
disp((Cp*Mu)/(k))
```

Press, Save and execute the function (Play button) in SciNotes window and then goto console window. Provide the input values to execute the above function as given below:

```
-->exec('C:\Users\asus\Desktop\prandtl.sce', -1)
Heat Capacity, (Btu/lbm deg. F) = 0.47
Viscosity, (lbm/ft h)=15*0.000672*3600
Thermal conductivity, (Btu/hr sq. ft)=0.065
Prandtl No. =
262.39015
```

Open SciNotes and type the following

```
Cp=input('Heat Capacity, (J/kg deg. C) = ');
Mu=input('Viscosity, (kg/m s)=');
k=input('Thermal conductivity, (J/s sq. m)=');
disp(' ');
disp('Prandtl No. =');
disp((Cp*Mu)/(k))
```

Press, Save and execute the function (Play button) in SciNotes window and then goto console window. Provide the input values to execute the above function as given below:

```
-->exec('C:\Users\asus\Desktop\prandtl1.sce', -1)
Heat Capacity, (J/kg deg. C) = 0.47*4184
Viscosity, (kg/m s)=15*0.001
Thermal conductivity, (J/s sq. m)=0.065*1.728
```

Prandtl No. =
262.61752

Exercise 3:

“Diffusion of water through stagnant, non-diffusing air”

Water in the bottom of a narrow metal tube is held at constant temperature of 293 K. The total pressure of air (assumed dry) is 1.01325×10^5 Pa (1.0 atm) and the temperature is 293 K (20 °C). Water evaporates and diffuses through the air in tube, and the diffusion path $Z_2 - Z_1$ is 0.1524 m (0.5 ft) long. Calculate the rate of evaporation at steady state in $\text{kg mol/s} \cdot \text{m}^2$. The diffusivity of water vapor at 293 K and 1 atm pressure is $0.250 \times 10^{-4} \text{ m}^2/\text{s}$. Assume the system is isothermal.

Data: $P_{BM} = 1.001 \times 10^5$, $P_{A1} - P_{A2} = 2.314 \times 10^3$ Pa

Solution

$$N_A = \frac{D_{AB} P}{RT(z_2 - z_1) P_{BM}} (P_{A1} - P_{A2})$$
$$N_A = \frac{(0.250 \times 10^{-4})(1.01325 \times 10^5)(2.314 \times 10^3)}{8314(293)(0.1524)(1.001 \times 10^5)} = 1.595 \times 10^{-7} \text{ kgmol/s} \cdot \text{m}^2$$

Open SciNotes and type the following

```
DAB=input('Diffusivity, (sq. m/s ) = ');
P=input('Total Pressure, (Pa)=');
PA=input('Vapor pressure of water at 20 deg.C. - Vapor
Pressure of Air at 20 deg.C, (PA1-PA2), (Pa)=');
R=input('Universal gas constant, (R) (cubic meter Pa/kg
mole K)=');
T=input('Temperature, (K)=');
Z=input('Diffusion path (Z1-Z2), (m)=');
Pbm=input('Log mean Pressure, (Pa)=');
disp(' ');
disp('Rate of evaporation at steady state. =');
disp((DAB*P*PA)/(R*T*Z*Pbm))
```

Press, Save and execute the function (Play button) in SciNotes window and then goto console window. Provide the input values to execute the above function as given below:

```
-->exec('C:\Users\asus\Desktop\prandtl1.sce', -1)
Diffusivity, (sq. m/s ) = 0.250*10^-4
```

Total Pressure, (Pa)= 1.01325×10^5

Vapor pressure of water at 20 deg.C. - Vapor Pressure of Air at 20 deg.C= 2.341×10^3

Universal gas constant, (cubic meter Pa/kg mole K)=8314

Temperature, (K)=293

Diffusion path (Z1-Z2), (m)=0.1524

Log mean Pressure, (Pa)= 1.001×10^5

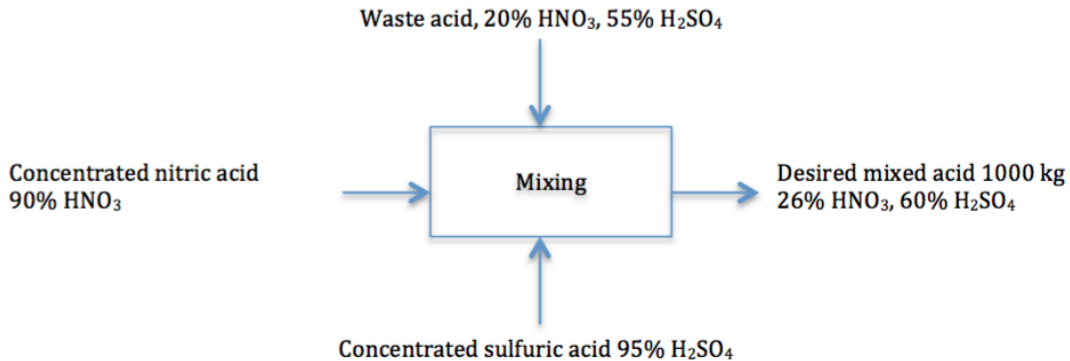
Rate of evaporation at steady state. =

0.0000002

The above result can also be written as $2E-07$ kg mol/s.m²

Exercise 4:

The waste acid from a nitrating process containing 20% HNO₃, 55% H₂SO₄ and 25% H₂O by weight is to be concentrated by the addition of concentrated H₂SO₄ containing 95% H₂SO₄ and concentrated HNO₃ containing 90% HNO₃ to get desired mixed acid containing 26% HNO₃ and 60% H₂SO₄. Calculate the quantities of waste and concentrated acids required for 1000 kg of desired mixed acid.



By overall Balance;

$$x + y + z = 1000$$

By H₂SO₄ balance;

$$0.55x + 0.95y = 600$$

By HNO₃ balance;

$$0.2x + 0.9z = 260$$

Write the above equation in the matrix form as given below

$$\begin{bmatrix} 1 & 1 & 1 \\ 0.57 & 0.95 & 0 \\ 0.2 & 0 & 0.9 \end{bmatrix} \begin{Bmatrix} x \\ y \\ z \end{Bmatrix} = \begin{bmatrix} 1000 \\ 600 \\ 260 \end{bmatrix}$$

Obtain the solution using SCILAB.

Open Console window in SCILAB and try the following

```
-->A=[1 1 1; 0.55 0.95 0.0; 0.2 0 0.9];
```

```
-->B=[1000 600 260]';
```

```
-->X=A\B
```

```
X =
```

```
400.
```

```
400.
```

```
200.
```

Exercise 5:

It is general practice in engineering and science that equations be plotted as lines and discrete data as symbols. Here is some data for concentration (c) versus time (t) for the photodegradation of aqueous bromine

t, min	10	20	30	40	50	60
c, ppm	3.4	2.6	1.6	1.3	1.0	0.5

The above data can be described by the following function

$$c = 4.84e^{-0.034t}$$

Use SCILAB to create a plot displaying both the data (using circle 'o' symbol).

Solution

Open Console window in SCILAB and try the following:

```
-->x=[10:10:60]'
```

```
x =
```

```
10.
```

```
20.
```

```
30.
```

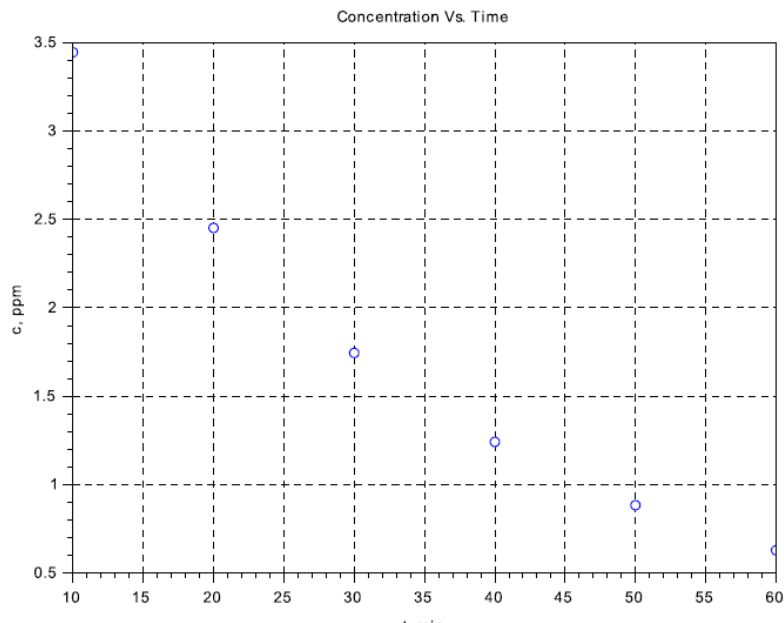
```
40.
```

```

50.
60.

-->y=[2.4,2.6,1.6,1.3,1.0,0.5]';
-->y=4.84*exp(-0.034*x);
-->plot(x,y,'o');
-->xgrid(1)
-->xlabel('t, min');
-->ylabel('c, ppm');
-->xtitle('Concentration Vs. Time')

```



Exercise 6:

The temperature dependence of chemical reactions can be computed with the

Arrhenius equation:

$$k = Ae^{-E/(RT_a)}$$

where k = reaction rate (s-1), A = preexponential factor (or frequency factor), E = Activation energy (J/mol), R = gas constant [8.314 J/mol . K], and T_a = absolute temperature (K). A compound has 1×10^5 J/mol and $A = 7 \times 10^{16}$ J/mol. Use SCILAB command window to generate values of reaction rates ranging for temperature ranging from 273 to 333 K. Use plot to generate a graph of $\log_{10}k$ versus $1/T_a$.

Open Console window in SCILAB and try the following

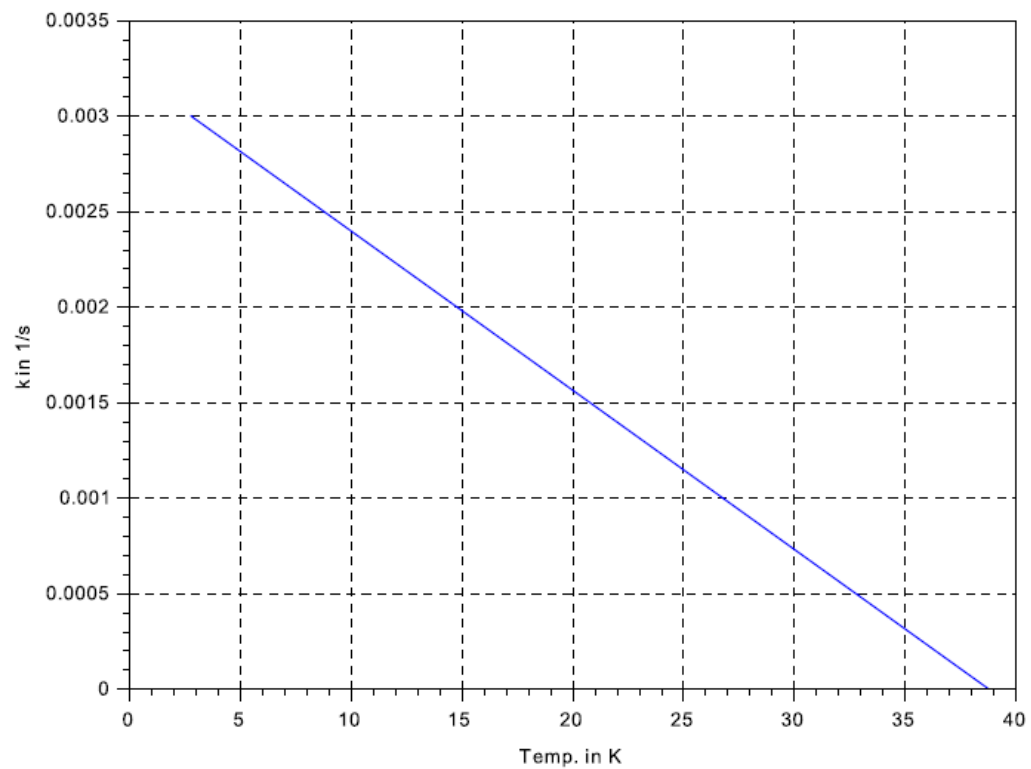
```

--> T=[273:10:333] '
T =

    273.
    283.
    293.
    303.
    313.
    323.
    333.

-->A=(7)*(10^16);
-->E=1*10^5;
-->R=8.314;
-->x=[(-10^5)/(8.314.*T)] '
-->k=[A*exp(x)] '
-->log1p(k);
-->1/T;
-->plot(log1p(k),1/T)
-->xgrid(1)
-->xlabel('Temp. in K')
-->ylabel('k in 1/s')

```



Exercise 7:

Find the specific volume of n-butane at 500 K and 18 atm using the Redlich-Kwong equation of state.

$$p = \frac{RT}{\hat{v}-b} - \frac{a}{\hat{v}(\hat{v}+b)}$$

$$\hat{v}^3(p) - \hat{v}^2(RT) + \hat{v}(a - pb^2 - RTb) - ab = 0$$

where

$$a = 0.42748 \left(\frac{R^2 T_c^2}{p_c} \right), \quad b = 0.08664 \left(\frac{RT_c}{p_c} \right),$$

take $T_c = 425.2$, and $p_c = 37.5$.

Solution

Open SciNotes and create the function file

```
function [y]=specvol(v)
Tc=425.2
pc=37.5
T=500
p=18
R=0.08206
aRK=0.42748*(R*Tc)^2/pc
bRK=0.08664*(R*Tc/pc)
y=p*v^3-R*T*v^2+(aRK-p*bRK^2-R*T*bRK)*v-aRK*bRK;
```

Console

```
-->v=0.2;
-->y=fsolve(v, specvol)
y =
    0.1404458
```

Note: The command `fsolve` is used to solve a nonlinear equation or model using an initial guess. Here the initial guess is $v=0.2$.

Example for `fsolve` command

Solve $F(x) = x^3 - 3x - 2$. Clearly the solution is 2 try the solution with SCILAB.

```
function [f]=F(x)
```

```

    f=x3-3*x-2
endfunction

```

Goto console

```

x = 100; //initial guess
-->x=100;

-->y=fsolve(x,F)

y =

    2.

```

Exercise 8: Use function command in SCINOTES and obtain the solutions for the problems listed in exercise 1a, 2a, 3a and

Exercise 1a: Reynolds number (SI Units)

Exercise 2a: Prandtl number (SI Units)

Exercise 3a: Diffusion of water through, non-diffusing air (SI Units)

Exercise 1a: Reynolds number

Open SciNotes and try the following:

```

function Nre=reynolds(D, V, Rho, mu)
    Nre=D*V*Rho/(mu)
endfunction

```

Press, Save and execute the function (Play button) in SCINOTES window and then goto console window. Provide the input values to execute the above function as given below:

Console window:

```

-->reynolds(3*0.0254,6*0.3048,0.08*16.018,0.015*0.001)

ans =

    11904.967

```

Exercise 2a: Prandtl number (SI Units)

Open SciNotes and try the following:

```

function Pr=Prandtl(Cp, Mu, k)
    Pr=Cp*Mu/(k)
endfunction

```

Press, Save and execute the function (Play button) in SCINOTES window and then

goto console window. Provide the input values to execute the above function as given below:

```
-->Prandtl(0.47*4184,15*0.001,0.065*1.728)
ans =
    262.61752
```

Exercise 3a: Diffusion of water through stagnant. Non-diffusing air (SI Units)

Open SciNotes and try the following:

```
function Na=diffusion(DAB, P, PA, R, T, Z, Pbm)
    Na=(DAB*P*PA)/(R*T*Z*Pbm)
endfunction
```

Press, Save and execute the function (Play button) in SCINOTES window and then goto console window. Provide the input values to execute the above function as given below:

```
-->
diffusion(0.250*10^4,1.01325*10^5,2.341*10^3,8314,293,0.1524,1
.001*10^5)
ans =
    0.0000002
```

Result

Thus we learned the use of SCILAB in solving algebraic equations in chemical engineering problems.