

CH0401 Process Engineering Economics

Lecture 4a

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Process Engineering Economics

1

Economic Analysis

2

Economic Balance in Cyclic Operation



Process Engineering Economics

- 1 Economic Analysis
- 2 Economic Balance in Cyclic Operation

Optimum proportions for a cylindrical container

The surface area (A) of the cylinder (closed) is given as the sum of the area of Sides, top and bottom covers of the cylinder

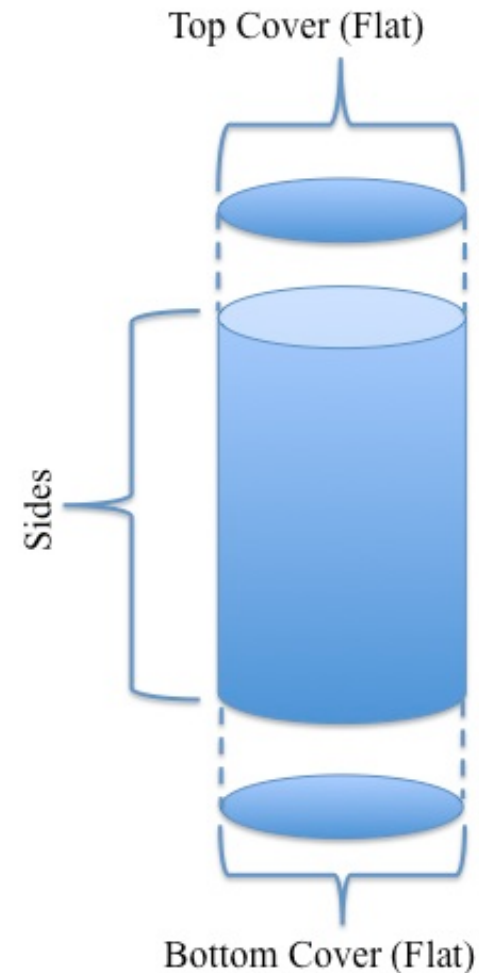
i.e.

$$A = (\pi \times D \times L) + \left(\frac{\pi}{4} D^2\right) + \left(\frac{\pi}{4} D^2\right)$$

$$A = (\pi \times D \times L) + 2\left(\frac{\pi}{4} D^2\right)$$

Where D = Vessel Diameter

L = Vessel Length (or Height)



Process Engineering Economics – *Economic Analysis*

$$A = (\pi \times D \times L) + 2\left(\frac{\pi}{4} D^2\right)$$

The above equation is minimized, simplified and solved to identify the minimum surface area required for cylinder with a given volume

$$f(D \times L) = (D \times L) + \left(\frac{D^2}{2}\right) \text{--- (A)}$$

For a given volume (V), the diameter and length are related by

$$V = \left(\frac{\pi}{4} \times D^2 \times L\right)$$

and

$$L = \left(\frac{4V}{\pi D^2}\right) \text{----- (B)}$$

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Now the equation (A) becomes

$$f(D) = \left(\frac{4V}{\pi D} \right) + \left(\frac{D^2}{2} \right)$$

Differentiating the above function and setting it to zero will give the optimum value for D

$$\left(-\frac{4V}{\pi D^2} \right) + D = 0$$

$$D = \sqrt[3]{\frac{4V}{\pi}}$$

From equation (B), the corresponding length will be

$$L = \sqrt[3]{\frac{4V}{\pi}}$$

Therefore, for a cylindrical container the minimum surface area to enclose a given volume is obtained when *length is made equal to the diameter*.

Example Problem: It is required to determine the optimum diameter to height ratio for a large oil storage vessel, so that the total cost is minimum. Following data may be used for the calculation

C_s = cost of sides per square meter

C_h = cost of the head or top per square meter = $1.5 C_s$

C_b = cost of the bottom per square meter = $0.75 C_s$

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The surface area (A) of the cylinder (closed) is given as the sum of the area of Sides, top and bottom covers of the cylinder

i.e.
$$A = (\pi \times D \times H) + \left(\frac{\pi}{4} D^2\right) + \left(\frac{\pi}{4} D^2\right)$$

Let C_T = total cost of the vessel
 D = Vessel Diameter
 H = Vessel Height

then

$$C_T = C_s(\pi \times D \times H) + C_b \left(\frac{\pi}{4} D^2\right) + C_h \left(\frac{\pi}{4} D^2\right) \text{-----(1)}$$

$$C_T = C_s(\pi \times D \times H) + (C_b + C_h) \left(\frac{\pi}{4} D^2\right) \text{-----(2)}$$

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$$V = \left(\frac{\pi}{4} \times D^2 \times H \right)$$

(or)

$$H = \left(\frac{4V}{\pi D^2} \right)$$

Substituting for equation H in equation (2) shown in slide 09

$$C_T = C_s \left(4 \frac{V}{D} \right) + (C_b + C_h) \left(\frac{\pi}{4} D^2 \right) \text{-----(3)}$$

Differentiating with respect to design variable D and equating to zero

$$\frac{dC_T}{dD} = \frac{-4C_s V}{D^2} + (C_b + C_h) \frac{\pi D}{2}$$

Process Engineering Economics – *Cyclic Process*

$$D^3 = \left[\frac{C_s}{C_b + C_h} \right] \times \frac{8V}{\pi} \text{-----(4)}$$

Substituting for the volume in (4) in terms of D and H gives the following optimum D to H ratio for the minimum cost of the vessel.

$$\frac{D}{H} = \frac{2C_s}{C_b + C_h} \text{-----(5)}$$

Substituting for C_b and C_h in terms of C_s gives the optimum D to H

$$\frac{D}{H} = \frac{2C_s}{(0.75 + 1.5)C_s}$$

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